

Discussion

## Exact equations for pipe-flow problems

By P.K. SWAMEE and P.N. RATHIE, Journal of Hydraulic Research, IAHR, 2007, 45(1), 519–528.

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The Authors are congratulated for solving a basic pipe flow problem. The Discussers would like to draw the attention to a point of interest.

Although the maximum error associated with Eq. (35) for  $D_*$  over the entire range of relative roughness,  $\varepsilon/D$ , and  $R$  = Reynolds number encountered in practice is slightly higher than 2%, it is limited to less than 0.6% for applications in practice. The error associated with Eq. (20) by using five terms of the series is relatively high. For example, Eq. (10) for  $\varepsilon/D = 0.001$  and  $R = 50,000$  yields  $f = 0.0240128$ , while using five terms of Eq. (20) yields  $f = 0.0190005$ , resulting in 21% error  $E$  defined as

$$E = \left| \frac{f_{(10)} - f_{(20)}}{f_{(10)}} \right| \times 100, \quad (36)$$

where the subscripts (10) and (20) refer to the equation number.

The deviations of Eq. (20) using five terms from that of Eq. (10) for the entire range of  $\varepsilon/D$  and  $R$  are plotted in Fig. D1. It indicates that the maximum error related to Eq. (20) reaches about 100%. Obviously, incorporating more terms in the series would improve the result but increase the floating point operations as well.

Sonnad and Goudar (2006) presented a relationship for the friction factor which was improved by the Discussers to

$$f = \left( a \ln \left( \frac{d}{(s - 0.28) \frac{s}{s+0.98}} \right) \right)^{-2}. \quad (37)$$

Here  $a = 0.8686$ ,  $d = 0.4587 R$ , and  $s = 0.1240 (\varepsilon/D)R + \ln(0.4587 R)$ . The errors associated with Eq. (37) over the entire practical range of  $\varepsilon/D$  and  $R$  are shown in Fig. D2 resulting in a maximum error of less than 0.04%. Although Eq. (37)

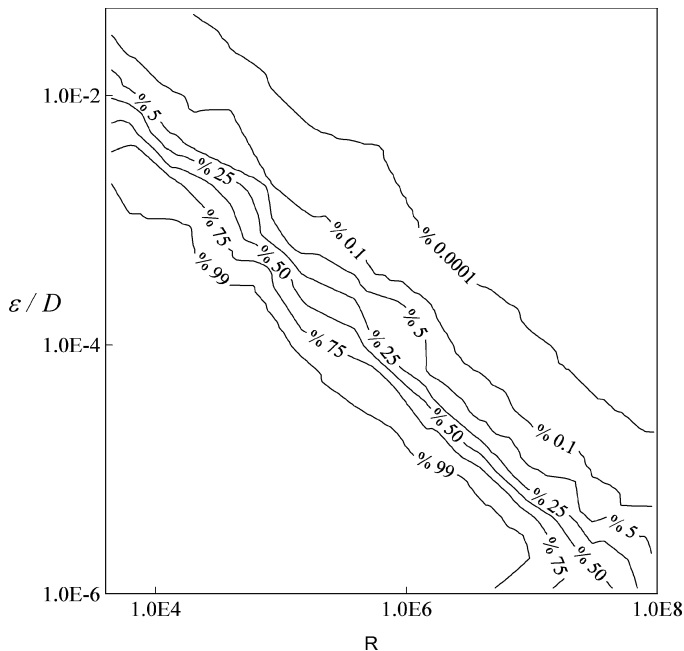


Figure D1 Error  $E$  associated with  $f$  based on Eq. (20) for the entire practical range of  $\varepsilon/D$  and  $R$

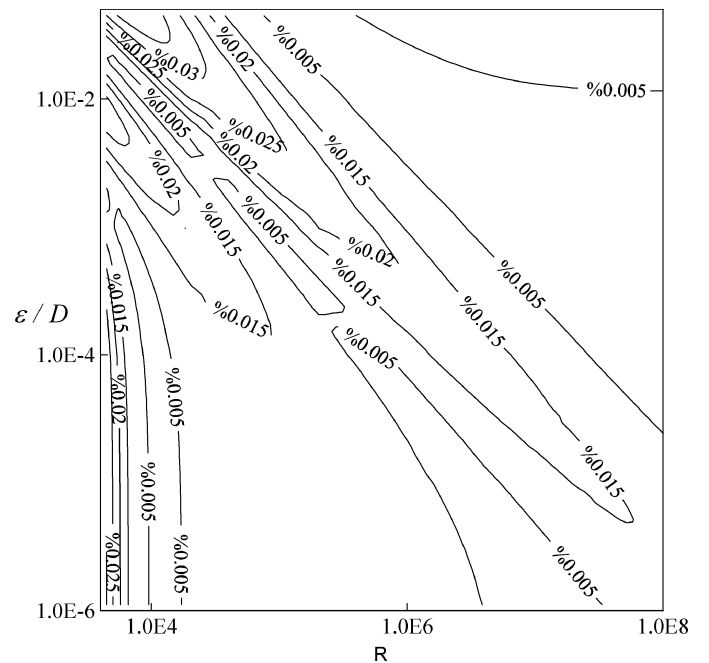


Figure D2 Error  $E$  associated with  $f$  based on Eq. (37) for the entire practical range of  $\varepsilon/D$  and  $R$